

1 We sincerely thank all of you for the detailed, thoughtful, and constructive comments and feedback. We have
2 incorporated all your suggestions in our paper, which has significantly improved from them. We elaborate below.
3 **Reviewer #2: (I)** Our algorithm can handle > 2 protected groups: in our numerical results, there are up to five protected
4 (racial) groups. It can also handle > 2 protected attributes (e.g., race, age, gender) by either: a) partitioning the
5 network based on joint values of the protected attributes, and imposing max-min fairness constraint for each group; e.g.,
6 constraints on (White, Young, Female) people, etc.; or b) imposing a max-min fairness constraint for each protected
7 attribute, separately. **(II)** We added a table of racial composition data for all networks. For instance, the MFP networks
8 consisted of 16.5% White, 35% Black, 21% Hispanic, 18.5% Mixed, and 9% Others. Each individual belongs to a single
9 race level. **(III)** The computational complexity of the problem increases exponentially with K , limiting us to increase K
10 beyond 3 for the considered instances. As demonstrated by our results, $K \sim 3$ was sufficient to considerably improve
11 fairness of the covering at moderate cost. **(IV)-(V)** Covering schemes are not inputs but rather *decision variables* of
12 the K -adaptability problem. The optimization problem will identify the best K covering schemes that satisfy all the
13 constraints including fairness constraints. **(VI)** In Section 5, we vary W from 0 to 1, in increments of 0.04; we employ
14 the largest W for which the problem is feasible (see lines 152-154). By construction, this choice of W guarantees
15 that all of the fairness constraints are satisfied. The choice of W varies with the network structure, no. of monitors,
16 no. of failed nodes and K . In Table 2, for network MFP2, and for $J = 1, \dots, 5$, W was: 0.64, 0.56, 0.48, 0.4 and 0.32,
17 respectively. We will report the values of W in a table in the appendix. **(V)** We clarify Figs. 2(b)-(d) by changing
18 the y-axis label to “Average normalized objective value” and adding to the caption that “it corresponds to the ratio of
19 objective value of the master problem (appendix, line 582) to the network size, averaged over the five network instances.”
20 **Reviewer #3 (I)-(II)** We incorporated all the recommendations. We included proof sketches, in the main text, after
21 Props. 1 and 2 and Th. 1. We improve clarity of Th. 1 by adding “In this formulation, there are two sets of variables: a)
22 The decision variables of the original problem; b) Dual variables emerging from employing linear programming duality
23 to reformulate the inner minimization problem in Problem (4)”. We explain the role of the dual variables, and the two
24 sets of constraints corresponding to different values of the parameter l . **(III)** The memory overflow is due to the fact that
25 the MILP formulation in Th. 1, although polynomial in all problem inputs, remains exponential in K . This is the main
26 motivation to develop the Bender’s decomposition approach in Section 4. Please see also response (III) to Reviewer #2.
27 **(IV)** We will provide a head-to-head comparison with Table 1. For instance, the corresponding results of our approach
28 ($K = 3$) for MFP2 network are: White: 56%; Black: 80%; Hispanic: 70%; Mixed: 71%; Other: 72%. **(V)** We improved
29 the K -adaptability formalization by adding to Section 4: “the MILP reformulation relies on three key components: a)
30 partitioning of the uncertainty set (achieved by introducing the parameter l), b) continuous relaxation of each subset of
31 the uncertainty set, and c) linear programming duality theory, to reformulate the robust optimization formulation over
32 each subset.” **(VI)** We will release the code and a “readme” file with instructions, detailing the sequence of the runs.
33 **(VII)** The 2-hour time limit is justified by the “flattening” in the “Objective Bound” (Figures 2(b)-(d)); this is a common
34 approach in optimization to terminate the algorithm when the change in objective is small. **(VIII)** We apologize for the
35 confusion caused by Line 281. We now write “... by imposing fairness constraints for each group. We set the number
36 of monitors to $I=N/3$.” Please see also our answer (VI) to Reviewer #2. **(IX)** We now add a section on future work. **(X)**
37 The Bernoulli distribution of the random variables Y_n and Z_{ni} is due to the Erdős-Rényi network generation process
38 (see lines 418-419). Therefore, the probability of Z_{ni} (similarly Y_n) taking the value of 1 is a known constant. **(XI)** The
39 “budget regime” refers to the assumptions on the values of I , which we made more explicit. **(XII)-(XIII)** The remaining
40 comments were addressed; we also added a part that was inadvertently deleted in the proof of Prop. 2.
41 **Reviewer #4 (I)** Please see answer (I) to Reviewer #2. **(II)** The paper [31] does not handle the uncertainty in node
42 availability, which is one of the main contributions of our framework. **(III)** We have added the discussion of the
43 worst-case PoF (Lemma 2) to the main text. **(IV)** We clarified, in the text, that we investigate the ratio of expected
44 coverage rather than expectation of ratios for analytical tractability. **(V)** The assumption on I can be interpreted as a
45 “small budget assumption” that helps simplify the evaluation of the coverage. Please also see answer (II) to reviewer #3.
46 **(VI)** Intuitively, uncertainty sets involving constraints as lower bounds on the (sums of) uncertain parameters satisfy the
47 upward-closeness property. We now provide three examples of such sets, that are of practical relevance. **(VII)** The value
48 of K determines the approximation quality, enabling the decision-maker to trade-off the optimality with computation
49 time. The choice of K is mainly guided by the available computational resources (e.g., time) and is domain specific.
50 Particularly, in low-resource settings (e.g., suicide prevention for homeless youth), we may be restricted to use low
51 values of K . **(VIII)** Please refer to answer (II) to Reviewer #3. **(IX)** We have incorporated all your comments to
52 improve the interpretability of Table 2. **(X)** Bender’s decomposition is an *exact* iterative algorithm that converges to an
53 optimal solution provided subproblems are LPs as in our case (Bertsimas, Dimitris, John N. Tsitsiklis. Intro. to linear
54 optimization, 1994). In practice, it is run until a termination criterion, such as time, optimality gap, etc. is satisfied. We
55 chose time limit for practical purposes. **(XI)** From discussion with our social work partners, $I \in [20, 30]\%N$ is typically
56 seen in the context of suicide prevention. We now have added more rows in Table 2, reporting the average coverage
57 improvement and average PoF for different values of I . For instance, for $I = 20\%N$, the average “Improvement in Min.
58 Fraction Covered” for $J = 0, \dots, 5$ is 17.2%, 13.8%, 14.0%, 10.0%, 9.0% and 6.7%, respectively. The “PoF” values
59 are all less than 4%. The value of γ can be inferred from J ($\gamma = J/I$), we replace “Size” with N in Table 2 for clarity.