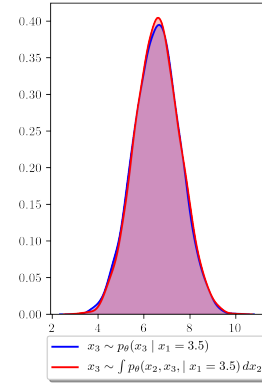


1 **Motivation of the method** Following Reviewer #3, we clarify the motivation behind NC. We emphasize our goal of  
 2 learning features from unsupervised data, useful for downstream tasks. This is the main point validated throughout our  
 3 experiments. We show that our paradigm of learning many conditional distributions of the data allows the extraction of  
 4 these unsupervised features from incomplete data, as well as arbitrary data imputations (inpaintings).

5 **General changes to the manuscript** Following Reviewer’s #1 suggestion, we included in the Appendix our experi-  
 6 mental protocols, architectures, and optimization parameter grids for all methods. We also added error bars to Tables 1  
 7 and 3 from the manuscript. Following Reviewer’s #3 suggestion, we tone down our claims about unsupervised learning.

8 **Regarding Sections 4.2 and 4.3** We apologize for the confusion brought by using the Donsker-Varadhan lower  
 9 bound as an objective for the discriminator. As pointed out by Reviewer #1, we acknowledge that the statement from  
 10 lines 188-190 is misleading. Our intent was to reason about optimal discriminators. Given an optimal discriminator, the  
 11 optimal NC minimizes the Jensen-Shannon divergence between  $p_{\theta^*}(x_r | x_a, a, r)$  and  $p(x_r | x_a, a, r)$ , where  $p_{\theta}$  and  $p$   
 12 represent the model and data distributions, respectively. Consequently, at optimality we have that  $D_{KL}(p||p_{\theta^*}) = 0$ ,  
 13 and thus the negative log-likelihood is equal to  $H(X_R|X_A)$ . Then, the more information  $X_A$  holds about  $X_R$ , the  
 14 lower the negative log-likelihood. Following Reviewer’s #1 and #3 remarks, we replace the Donsker-Varadhan lower  
 15 bound by one in terms of the Jensen-Shannon divergence, merging Sections 4.2 and 4.3, removing the misleading  
 16 statement from lines 188-190, making clear that our reasoning follows for optimal discriminators and NC’s, and making  
 17 the variables on which the different distributions depend explicit. We thank the reviewers for their careful reading.

18 **Regarding conditional distributions consistency** We thank Reviewer #1 for bringing  
 19 this subtle point to our attention. We now provide a proof about the consistency of  
 20 conditional and marginalized densities in our Appendix. The proof sketch goes as  
 21 follows: if we assume that the data has support on a compact set  $\Omega$ , and that the NC  
 22 is trained to optimality, then, writing  $\lambda$  for the Lebesgue measure on  $\Omega$ , we can show  
 23 that  $D_{JS}(p_{\theta}(x_S | x_A) || \int p_{\theta}(x_S, x_{R-S} | x_A) \lambda(dx_{R-S}))$  is small by leveraging the  
 24 triangular inequality of the distance on probability measure on  $\Omega$  defined by the square  
 25 root of the Jensen-Shannon divergence. We then use Jensen’s inequality with uniform  
 26 weights  $\frac{1}{\lambda(\text{supp}(X_{R-S}))}$  to bound the distance between the model and data marginalized  
 27 distributions by the integral of the distance between the model and data conditional  
 28 distributions. We leave the theoretical analysis for the case for non-compact supports to  
 29 future work. Moreover, we illustrate this consistency between conditional and marginalized  
 30 densities empirically, here in the Figure on the right.



31 **Better empirical comparison against VAEAC** As suggested, we improve our empirical  
 32 comparison against VAEAC and update the manuscript with the results shown here in Table 1 (Left, semi-supervised  
 33 learning results on SVHN), and Table 1 (Middle, missing data imputation on three UCI datasets).

34 **Improved performances on the missing data imputation task** As requested by Reviewer #3, Table 1 (Middle)  
 35 shows substantially improved missing data imputations results for our model. This results were obtained after fixing a  
 36 bug in our code.

37 **Performance degradation depending on train/test masks mismatch** We follow Reviewer’s #1 suggestion to  
 38 analyze the performance of NC as a function of the mismatch between train and test masks. To this end, we report the  
 39 RMSE between  $X_R$  and  $\hat{X}_R$  on the UCI/Letter dataset. We consider four different scenarios: (i) masks observed during  
 40 training applied on train data, (ii) masks observed during training applied on test data, (iii) masks unobserved during  
 41 training applied on train data, and (iv) masks unobserved during training applied on test data. Results in Table 1 (Right).

| Algorithm | Test error (%)     | Algorithm | Spam                | Letter              | Credit              | Masks/Data | Train        | Test         |
|-----------|--------------------|-----------|---------------------|---------------------|---------------------|------------|--------------|--------------|
| VAEAC     | 57.89 ± 1.01       | GAIN      | .0513 ± .002        | .1198 ± .005        | .1858 ± .001        | Train      | .0891 ± .001 | .0896 ± .001 |
| NC        | <b>17.2 ± 0.59</b> | VAEAC     | .0552 ± .002        | .1115 ± .001        | .1523 ± .002        | Test       | .0897 ± .001 | .0901 ± .001 |
|           |                    | NC        | <b>.0486 ± .001</b> | <b>.0851 ± .002</b> | <b>.1276 ± .002</b> |            |              |              |

Table 1: **(Left)** Semi-supervised learning on SVHN using 1000 labels. **(Middle)** RMSE for missing data imputation on UCI datasets. **(Right)** RMSE on UCI/Letter using train/test data/masks.