- To Reviewer 1 Thanks for your comments and questions. It seems you misunderstood some key points and details.
- Hope our explanation below could help to clarify some misunderstandings and confusion.
- (1) Theorem 2 in [Maurer 2005] is totally different for our Theorem 2, although they may look similar. Theorem 2 3
- in [Maurer 2005] is the generalization bound for Single Task Learning (ordinary supervised learning), which certainly
- depends on the sample size m (number of samples in the task). Actually, this bound is from [Bousquet and Elisseeff
- 2002]. In contrast, Theorem 2 in our paper is the generalization bound for *Meta-Learning* with S/Q training, which is
- independent of the sample size m of each task but depends on the total number of tasks n. To our knowledge, this is the
- first sample-size-free bound for meta-learning.
- (2) The empirical evaluation corroborates our theoretical claims. By "specific learning rate schedule", we think
- you meant the learning rate should satisfy $\zeta_t \leq c/t$ for a constant c and $t = \{1, \dots, T\}$ where T is the total number of 10
 - training steps, as stated in Theorem 3 in the Appendix. Notice that this condition can be easily satisfied with a fixed
- learning rate in practice. For example, ProtoNets with a fixed learning rate $\zeta_t = 1e 3$ converges in 24,000 episodes 12
- (T=24,000) and satisfies the condition with c=240. Actually, Hardt et al. (2016) also conducted experiments with a 13
- fixed learning rate 1e-2 and a constant number of training steps to verify their theory. 14
- We would like to reiterate that our empirical evaluation is conducted with most popular meta-algorithms including 15
- MAML [Finn et al. 2017], ProtoNets [Snell et al. 2017] and Bilevel programming [Franceschi et al. 2018] by strictly 16
- following their training details on standard benchmarks (few-shot classification on mini Imagenet and sinusoidal few-shot 17
- regression). We think the empirical evidence is sufficient to verify our theoretical claims.
- (3) Our results are not contradictory to those in [Triantafillou et al. 2020]. Notice that generalization gap \neq
- test error. In fact, generalization gap = test error training error (see [1] [2] for further reading). It is entirely possible 20
- that test error keeps decreasing while generalization gap remains unchanged, because training error can also be 21
- decreasing. This is exactly the case here. Fig. 2(b) in [Triantafillou et al. 2020] shows that the increase of shots 22
- (inner-task sample size) reduces test error, which is evidently true. However, the increase of shots also reduces training 23
- error, and both our theoretical bound and empirical evaluation show that the generalization gap keeps unchanged for 24
- S/Q training. 25

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- [1] Understanding Machine Learning: From Theory to Algorithms. Shai Shalev-Shwartz and Shai Ben-David. 2014. 26
- [2] Predicting the Generalization Gap in Deep Networks with Margin Distributions. Yiding Jiang, Dilip Krishnan, Hossein Mobahi, 27
- Samy Bengio. ICLR 2019. 28
- (4) For your other comments: 1) The inner-task gap vanishes because the expectation of the loss function w.r.t. 29
- a new sample $z \sim \mathcal{D}$ is the same as that w.r.t. a new sample set $S^{ts} \sim \mathcal{D}^q$. In particular, inner-task 30
- gap of S/Q training: $\mathbb{E}_{\mathcal{D},S^{tr},S^{ts}}[\mathbb{E}_z l(h,z) \hat{L}(h,S^{ts})] = \mathbb{E}_{\mathcal{D},S^{tr}}[\mathbb{E}_{S^{ts}}[\mathbb{E}_z l(h,z)] \mathbb{E}_{S^{ts}}[\frac{1}{q}\sum_{z_j\in S^{ts}}\hat{l}(h,z_j)] = \mathbb{E}_{\mathcal{D},S^{tr}}[\mathbb{E}_z l(h,z) \frac{1}{q}\sum_{z_j\in S^{ts}}\mathbb{E}_{z_j}l(h,z_j)] = \mathbb{E}_{\mathcal{D},S^{tr}}[\mathbb{E}_z l(h,z) \mathbb{E}_z l(h,z)] = 0.$ 31
- 2) The statements regarding the generalization bounds of LOO loss $\epsilon(n,\beta,\tilde{\beta})$ and S/Q loss $\epsilon(n,\beta)$ are not contradictory. When we say both of them are determined by the uniform stability β of the meta-algorithm, we did not mean "solely 33
- 34
- determined". The former also depends on the uniform stability $\tilde{\beta}$ of the inner-task algorithm but the latter does not. 35
- 3) Chen et al. (2019) did not use "batch multi-task training" as you mentioned, which is a traditional way for training 36
- meta-algorithms as used in [Maurer 2005]. They simply trained an ordinary supervised classifier and compared it with 37
- S/Q trained meta-algorithms. They never compared or discussed different training schemes for meta-algorithms. 38
- 4) The notation \bar{w}_t is defined in line 157. 39
- To Reviewer 2 Thanks for your comments and suggestion. The results of LOO training were previously put in a 40
- separate section, but due to space limitation, we merged them with the results of S/Q training. We will reorganize the 41
- paper in the final version where more space will be given.
- To Reviewer 3 Thanks for your comments and feedback. Reptile is an inspiring meta-algorithm which does not need a 43
- S/Q split for training but still achieves comparable performance with MAML. To make the traditional generalization
- bound apply to Reptile, we may first need to derive the randomized uniform stability of Reptile w.r.t. its update rule, 45
- which is not equivalent to "meta-level SGD". We think it would be very interesting to study the generalization of Reptile 46
- and will add more discussion in the revised version. Thank you for bringing that up. 47
- To Reviewer 4 Thanks for your comments and feedback. Indeed the discussion of LOO meta-training is not related to
- Theorem 4 in our paper, but we introduce LOO meta-training because it is "a surrogate to the traditional scheme that is 49
- compatible with gradient-based and metric-based meta-learning algorithms" (Reviewer 3 said it nicely and we quote). 50
- Besides, it is a nice comparison to S/Q training in terms of generalization bounds. We will further clarity this in the 51
- final version.