

1 We thank all reviewers for their constructive feedback.

2 **Techniques (Reviewer 2) and comparison to the concurrent work of [DKTZ20] (Reviewer 1):**

3 1. We propose to sequentially minimize a series of “potential functions” $f_{u,b}(w)$ (see Appendix F for definition)
4 for progressively smaller values of b . We believe that our time-varying setting of parameter b in combina-
5 tion with this new potential function is the key to achieve the state-of-the-art $O\left(\text{poly}\left(\frac{1}{1-2\eta}, \log \frac{1}{\epsilon}\right)\right)$ label
6 complexity for active learning under Massart noise, which has not appeared before.

7 2. We also believe that our application of online linear optimization in (active) learning halfspaces is quite
8 novel: in order to optimize $f_{u,b}(w)$, we construct an online linear optimization problem whose *negative*
9 *benchmark performance* is an upper bound of $f_{u,b}(w)$ (Lemma 6)! To the best of our understanding, the
10 work of [DKTZ20] considers optimizing the global expectation of a sigmoid-like loss function (denoted as
11 $L(w)$), and its key observation is that the gradient of the expected loss $\nabla L(w)$ is large whenever w and u
12 have a large angle. We are not sure if there is a connection there (although any connection would be very
13 interesting). To efficiently solve the online linear optimization problem in a sparsity-adaptive manner, we use
14 online mirror descent with a squared ℓ_p -norm regularizer (with p close to 1), which is well-known to promote
15 attribute-efficiency in prior works on online learning.

16 We will add more discussions and explanations on the above points in the final version.

17 As Reviewer 3 suggests, we will add a brief introduction to online mirror descent in the final version. The extra hard
18 thresholding step suggested by the reviewer is not necessary (although it would not hurt either - the final error guarantee
19 would only change by a constant factor); we refer the reviewer to the proof of Theorem 4 for more details.

20 **References**

21 [DKTZ20] Learning Halfspaces with Massart Noise Under Structured Distributions, Diakonikolas, Kontonis, Tzamos,
22 Zarifis, arXiv:2002.05632