

1 We thank the reviewers for their valuable feedback.

2 [R1-More analysis of global landscape on LSGAN, WGAN, etc.](#): 1) Note Remark 1 (L155): the results can be extended  
 3 to a class of separable GANs and relativistic GANs (R-GANs). More specifically, Thm. 3 (L1501) and Thm. 4  
 4 (L1513) show that separable GANs in Eq. (30) have bad basins while R-GANs in Eq. (31) have no bad basins. These  
 5 results only require minor conditions on the loss (Assumption J.1-J.5), covering logistic loss, hinge loss, squared  
 6 loss, etc.; 2) To cover LS-GAN (min-max version), two minor changes suffice: change the two  $h$  functions to  $h_1$   
 7 and  $h_2$  in Eq. (30); change Assumption J.1-J.3 accordingly. We'll modify to include LS-GAN and R-LS-GAN. 3)  
 8 W-GAN is difficult to analyze. See App. J.2 for a discussion. The difficulty also indicates that our contribution goes  
 9 beyond a global landscape analysis in that we identify the losses (R-GANs) that are amenable to rigorous analysis.

10 [R1&R4-Experiments to validate proposed GAN losses.](#) As stated in L230, “the  
 11 effectiveness of relativistic GANs has been justified (to some extent)” and “our  
 12 goal is to use experiments to support the landscape theory.” For this, we focus  
 13 on: a) **advantage in narrow nets**; b) **robustness to initialization**. Our paper  
 14 validates a) and b) in four ways: **1)** On L265-269 we show that for MNIST and a  
 15 certain initial point, RS-GAN outperforms JS-GAN by 30 FID scores (around 30  
 16 vs. 60). **2)** On L256, we show RS-GAN outperforms JS-GAN by 9 FID scores  
 17 (45 vs. 53) when using a ResNet (bottleneck) on STL. **3)** In Tab. 11 (in appendix)  
 18 we show that R-hinge-GAN outperforms hinge-GAN with 1/4 width (24 vs. 33  
 19 FID on CIFAR10). Both SN-GAN and BigGAN papers use hinge-GAN, so we  
 20 check hinge loss. **4)** In experiments (Tab. 2, Tab. 11 in paper), separable versions (JS-GAN, hinge-GAN) do not beat  
 21 their relativistic counterparts (RS-GAN, R-hinge-GAN) in any case. These points show: R-GANs are more robust to  
 22 initialization and architecture. In new experiments we show: **5)** R-LS-GAN outperforms LS-GAN by 6 FID (42 vs. 48)  
 23 with 1/4 width (Tab. 1 below); **6)** RS-GAN outperforms WGAN-GP (Tab. 2 below); **7)** experiments on LSUN (higher  
 24 resolution than CIFAR10 - Fig. 1). These new experiments further justify the advantage of R-GANs. We will explain in  
 25 the main text.

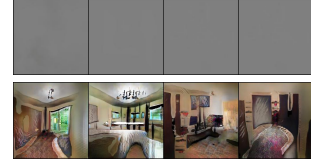


Figure 1: LSUN (256×256) generation with CNN structure for JS-GAN (above) and RS-GAN (bottom).

26 [R2-existence of reachable path doesn't mean SGD can follow it; there are still questions.](#) There're two branches of re-  
 27 sults for neural nets: one branch [60,43] only discusses paths and basins assuming width  $n$ . A drawback, as you point  
 28 out: convergence of GD is not proved. Nevertheless, this is enough to distinguish RS and JS-GAN. Another branch  
 29 [2,25,37] proves convergence of SGD assuming width  $\geq n^6$ . Drawback: assumption of width  $n^6$  is impractical. An  
 30 ideal result that SGD converges for width  $n$  is a huge open question for neural nets (attempts exist, but all have strong  
 31 limitations). We do not intend to solve this open question here. We combine Thm. 1,2 with the first branch since it is  
 32 cleaner and already non-trivial. It is possible to combine with the second branch (on convergence), but it will make this  
 33 paper much longer. Future advances for neural nets can be potentially combined with our function space result.

34 [R2-parameterized result is vague. More detail of connections. and](#)  
 35 [R3-Intuition on proof of Prop. 1,2; how proof differs from supervised learning.](#) The proof strategy of Prop. 1,2 is an  
 36 adaptation of those of [60,43,59] to GANs. References [60,43,59] consider a convex loss (e.g. quadratic) in function  
 37 space and “transfer” decreasing paths in function space to decreasing paths in parameter space. To achieve this “transfer,”  
 38 some assumptions on the architecture (e.g. width large enough) are needed [60,43,59]. We apply this approach to the  
 39 GAN loss. In our proof, we state the general requirement of “transfer” in Assumption I.1-I.3, and then prove when these  
 40 assumptions hold in Appendix I.2 and I.3 (using architecture assumptions of [60,43,59]). We'll discuss in the main text.  
 41 [R3-proof sketch of Thm. 1, Thm. 2.](#) For Thm. 1, careful computation suffices. For Thm. 2, we build a graph with nodes  
 42 being input data, decompose the graph into cycles and trees, compute the loss by grouping the terms according to cycles  
 43 and trees, and add each term. We'll sketch the proof in the main text.

44 [R4-study WGAN.](#) Thanks for suggesting. i) See the first response, point 3) in L8 of the rebuttal. ii) We add simulation  
 45 showing that RS-GAN outperforms WGAN-GP for standard datasets (Tab. 2 below).

46 [R4-study DRAGAN architecture.](#) Thanks for pointing out the reference, which we read with great interest. It suggested  
 47 that mode collapse may be due to bad equilibria. However, there is no formal statement or proof. We will cite it and  
 48 discuss the connection with our work. DRAGAN adds a penalty of the gradient which may help eliminate some basins,  
 49 but it likely creates other basins. A formal analysis requires much effort, and is an interesting future direction.

50 [R4-Sec. 3 \(two-cluster\) a bit redundant with analysis of 2-point distribution.](#) Thanks. The analysis of a 2-point distri-  
 51 bution is about the landscape, not the training process. In contrast, Sec. 3 shows that the basin really appears in training,  
 52 and the theoretical values 0.48 and 0.35 really play a role in understanding the training process. Following your  
 53 comment, we will reduce the length of Sec. 3.

	Regular channel/2	channel/4
LS-GAN	<b>32.93</b>	37.83 48.63
R-LS-GAN	34.78	<b>34.34</b> <b>42.86</b>

Table 1: FID results on CIFAR-10 for LS-GAN and R-LS-GAN with CNN structure given in Tab. 5 of the appendix.

		Regular channel/2	channel/4
CNN	WGAN-GP	39.66	42.39 50.56
	RS-GAN	<b>27.16</b>	<b>32.74</b> <b>49.74</b>
ResNet	WGAN-GP	21.33	23.80 40.45
	RS-GAN	<b>19.31</b>	<b>21.78</b> <b>31.26</b>

Table 2: FID results on CIFAR-10 for WGAN-GP and RS-GAN with CNN and ResNet.