- We thank the reviewers for their thoughtful reviews; below we address their main concerns. While it only impacts our
- LSVI analysis and our analysis of FRANCIS remains unchanged, we wish to note that in our own internal re-review we
- found a small error in the proof of Lemma 23. We apologize for this. Fortunately we can address it by a relatively small
- change: to define inherent Bellman error using the, perhaps more common, ∞-norm, i.e., if eq 2 (def 1) reads

$$\mathcal{I}_{\mathbb{E}} = \max_{Q_{t+1} \in \mathcal{Q}_{t+1}} \min_{Q_t \in \mathcal{Q}_t} \max_{(s,a)} |[Q_t - \mathcal{T}_t^P(Q_{t+1})](s,a)|. \tag{*}$$

- This allows us to express the misspecification error (e.g., eqn 37 in appendix) directly in every (s, a) pair, as opposed to
- in expectation, and the concentration argument in Lemma 23 (which is a concentration argument on deviation of the
- encountered features wrt their expectation) is no longer needed. Note all the results of the paper continue to hold when
- using the ∞ -norm misspecification error in equation (\star) above. 8
- **Explorability** (R1, R2, R4). We are sorry for the lack of clarity and we are happy to address our explorabil-9 ity assumption and the relation to Chi et al's bounds. Our analysis gives guarantees for the algorithm under 10 two sets of distinct assumptions, which we called *implicit* and *explicit* regularity in the paper (see def. 6 in app.). 11
- 1) Under *implicit* regularity, we do not put assumptions on the norm of reward parameter $\|\theta^r\|_2$, but only a bound on 12 the expected value of the rewards under any policy: $|\mathbb{E}_{x_t \sim \pi} r_t(x_t, \pi_t(x_t))| \leq \frac{1}{H}$, (see line 762 in appendix). This representation allows us to represent *very high rewards* ($\gg 1$) *in hard-to-reach states*. It basically controls how big the 13 14 value function can get. This setting is more challenging for an agent to explore even in the tabular setting and even in 15 the case of a single reward function. If a state is hard to reach, the reward there can be very high, and a policy that tries to go there can still have high value. Under this implicit regularity assumption, the explorability parameter would show 17 up for tabular algorithms as well (as minimum visit probability to any state under an appropriate policy): the classical 18 assumption that $|r(s,a)| \le 1$ would be replaced by $|r(s,a)| \le 1/\nu_{min}$, and the reward / transition noise would become 19 $1/\nu_{min}$ subgaussian; this would ultimately command a corresponding $1/\nu_{min}$ increase in sample complexity even for 20 tabular algorithms in the fixed reward setting as well as in the reward free setting. Note that the results from Chi et al. 21 are derived under bounds on the reward parameter which do not satisfy this setting, and therefore our lower bounds are 22 not incompatible with their prior results for the tabular setting.
- 2) Under explicit regularity (Definition 6 in the appendix) we do make the classical assumption that bounds the 24 parameter norm $\|\theta^r\|_2 \le 1/H$ (line 767 in appendix). In this case, our lower bound no longer applies, but the proposed 25 algorithm still requires good "explorability" to proceed (in contrast to, e.g., LSVI-UCB as several reviewers have noticed). We then completely agree with R1, R2 and R4 that the assumption should not be necessary in this case, and 27 removing it is certainly very important, but given the already existing challenges brought by the inherent Bellman 28 error setting we have to leave this as future work. Nonetheless, we would like to point out that explorability does not 29 make the exploration problem trivial. A random policy (i.e., \(\epsilon\)-greedy) can still take exponential time to learn; other 30 authors [1, 5] have made similar or even stronger assumptions (a bound on the minimum visit probability to any state) 31 to proceed in the context of function approximation. 32
- Layer-by-layer learning (R4) As the reviewer suggests, an algorithm that is able to learn all layers together might be more horizon efficient. Interestingly, with our approach we do already achieve the same horizon dependence as the state 34 of the art [3] for tabular RL at the time of submission $O(S^2AH^5/\epsilon^2)$ (see also table 1 in our manuscript). 35
- Motivation (R4) With this work our aim was to try to weaken the assumptions the current literature makes in the 36 exploration setting with linear function approximation. Although the minimum set of assumptions for RL to work are 37 not well understood even in the linear case [2], our objective is to at least have algorithms that work under assumptions 38 typically made in the batch setting, i.e., when mainstream batch algorithms like least square value (or policy) iteration 39 work [6, 4] using already collected data. We consider this work as a first step in this direction.
- Clarity (R2) We thank the reviewer for highlighting the clarity issue, and we do plan to use the extra page that is 41 allowed for the camera ready to expand the motivation behind the algorithm, to give a more detailed proof sketch and to 42 43 clarify the role of explorability, which is especially important as the algorithm style is different than those presented in a number of recent theoretical papers.

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