- We thank the reviewers for their insightful feedback. We are encouraged that they found our motivation and idea to
- be novel (R2, R4), practical (R1), interesting (R3) and scalable (R2, R4). Moreover, we are grateful that reviewers
- identified our contributions beyond just performance gains on different tasks (R1, R2, R4), and that R2 appreciated our
- theoretical contributions. Reviewers also found that our empirical studies are sound and convincing (R2, R4).
- Below we first provide a recap on the goal of our work, and then give a point-by-point response to the comments.
- [Recap] What is our goal? We investigated the role of sparsity and DAG constraints for learning linear DAGs,
- and established the corresponding asymptotic guarantees. Inspired by that, we formulate a likelihood-based method
- (GOLEM), and showed that one only has to apply soft sparsity and DAG constraints for structure learning.
- @R1, R4 Performance metrics: Thank you for raising this issue. Following your suggestions, we have computed
- and will report the normalized SHD and Structural Intervention Distance (SID) in the revision. We found that these new 10
- metrics yield consistent observations with the existing metrics reported in the paper. 11
- @R2, R4 Real data experiment: Thank you for the suggestion. We agree that these methods may not learn much on 12
- the Sachs dataset; in fact, even nonparametric extensions of NOTEARS, e.g., GraN-DAG (Lachapelle et al., 2020), do 13
- not perform well on this dataset, either. Given your comment, we have done and will include an additional experiment 14
- based on SynTReN generator (Van den Bulcke, 2006), which simulates gene expression data with ground truth. For 15
- each method, the SHDs, normalized SHDs and SIDs are: GOLEM-NV (35.9, 1.8, 128.4), GOLEM-EV (42.8, 2.1, 16
- 139.4) and NOTEARS-L1 (48.7, 2.4, 162.6), respectively. Note that lower is better for all three metrics reported here.
- @R1 Assumption of linearity: Great point. Learning DAGs is challenging, and some assumptions (e.g., linearity) are needed for developing estimation methods and corresponding theoretical guarantees, as in LiNGAM and NOTEARS. 19
- We plan to extend our method to nonlinear cases as future work (L372-373). 20
- @R1 "Regularization" vs. "soft constraint": Thank you for pointing this out. In order to avoid any possible 21
- confusion, we will follow your suggestion and replace the term "regularization" with "soft constraint" in the final paper. 22
- @R1 Assumption of DAGs: We agree that it is a huge assumption and will make it explicit in all relevant sections. 23
- @R1 Using a more effective variant of PC: We experimented with the original PC and its variant CPC (Conservative 24
- PC), and picked the latter which gave better results. We will include the detail in the revised paper. Thank you. 25
- @R2 Choice of regularization coefficients: Thank you for the insightful comment. For NOTEARS-L1, we 26
- experimented with several choices, and picked the one which yielded the best results (L570-573). For GOLEM, our 27
- focus is not to attain the best possible accuracy with the optimal hyperparameters, but rather to empirically validate our 28 theoretical results. We thus did not perform a thorough hyperparameter search, and found that small coefficients suffice
- to work well (L588-590). We will include more details on this. 30
- @R2 Proof of Lemma 1: We will include the proof in the final version. Thank you. 31
- @R2 Regularization coefficients in asymptotic proof: Thanks a lot for this suggestion, which helps improve our 32
- presentation. We chose the sparsity term such that it scales with the order of $\mathcal{O}(\log n/n)$, as in the consistency result of 33
- BIC score. We will clarify this in the revised paper before Theorem 1 (L153). 34
- @R3 "puts much emphasis on beating NOTEARS" and "comes with no little surprises for more optimal ML 35
- loss is used rather than square loss from NOTEARS": Thank you for the comment. We would like to respectfully 36
- remind R3 that our main contributions include establishing the asymptotic guarantees and showing that soft DAG 37
- constraint is, under mild assumption, sufficient to recover the underlying DAGs (Section 3.1). The superior performance 38
- of GOLEM came as a by-product of our theoretical results.
- @R3 "transforming DAG constraint into a penalty is such an advantage w.r.t. NOTEARS is questionable"
- and "Is there a more efficient way for implementing constraint minimization than augmented Lagrangian": 41
- We would like to make it clear that our method *does not* involve augmented Lagrangian, since we proposed an easier 42
- unconstrained problem with a soft DAG constraint term (L213-216). This is entirely different from the constrained 43
- formulation of NOTEARS which increases the penalty to very large values, leading to optimization difficulties (L79-81). 44
- We also provided asymptotic guarantees and extensive empirical results to justify our motivation. 45
- @R3 Impact of sparsity on NOTEARS: It already includes a sparsity term, denoted as NOTEARS-L1 in Section 5. 46
- @R4 Causality and broader impact section: Thanks for pointing this out. We will remove the claim of "causality". 47
- @R4 Use of SHD: We use SHD to measure the discrepancy between DAGs, and SHD-CPDAG for equivalence 48
- classes (L624-628), which is what R4 nicely suggested. We will make these terminologies clear in the revised version. 49
- We hope that the above discussion has addressed the reviewers' concern, and will incorporate all suggestions in the
- final version. We once again appreciate the reviewers' time dedicated to reviewing our paper.