

1 We thank all reviewers for their time taken to review our work and their helpful comments and suggestions to improve  
2 this work. As a recap, in our work we studied the problem of returning all  $\epsilon$ -good arms. We establish lower bounds for  
3 the hardness of this problem and present two algorithms with theoretical guarantees, FAREAST and (ST)<sup>2</sup>. The former is  
4 asymptotically optimal on all instances. Additionally, via a novel moderate confidence bound, we are able to show that  
5 the latter, which enjoys great empirical performance, is optimal in many settings, such as the common  $\delta = 0.05$ . Below,  
6 we respond to individual review comments individually.

7 **Reviewer 1:** Thank you for your review. Addressing your comment about weaknesses and novelty: The core challenge  
8 of this work stems from the need to estimate the threshold  $\mu_1 - \epsilon$  to sufficient precision which is new to this problem.  
9 This motivates our algorithms and affects our lower bounds. In particular, we develop a new theoretical technique for  
10 the lower bound in Appendix D to handle this that may be of independent interest. We will highlight this in future  
11 drafts to make this apparent. Thank you for the note about the abstract. We will be sure to clarify that the nature of our  
12 results are to provide sample complexity bounds. Thank you for pointing out the confusion regarding Figure 4a. In the  
13 sample data, there were 2.2M total ratings used to estimate the means. Before this number of samples, we draw the  
14 performance curves of each algorithm as a solid line, and after this point as a dashed line. This was to highlight that  
15 (ST)<sup>2</sup> would have performed better in practice as well even at 2.2M ratings. We will clarify this in the final version.

16 **Reviewer 2:** Thank you for your careful read and comments about our paper. Regarding the lower bounds, Theorem  
17 2.1 follows using standard techniques. To prove Theorem 4.1 however, in section D.2 we develop a novel technique  
18 that allows one to reduce a more general composite hypothesis test to the more limited set of tests covered via the  
19 Simulator lower bounding technique of [1], and this may be of independent interest. We will highlight and expand  
20 upon this in future drafts to make it more readily accessible. Regarding more general distributions for the lower bound:  
21 for Gaussians of unknown variance  $\sigma^2$ , the lower bound of Theorem 2.1 still applies (with an additional factor of  $\sigma^2$ ).  
22 Intuitively this is since the known variance case should be an easier problem. Whether it is possible to achieve this  
23 bound or if a tighter bound can be proven when  $\sigma$  is unknown is an interesting question for future work. For distributions  
24 beyond Gaussians, the result can easily be altered for any distribution with a well defined mean. In this case, terms  
25 such as  $(\mu_1 - \epsilon - \mu_i)^2$  present in the bound will be replaced by KL-divergences between the appropriate distributions.  
26 Finally, we agree that a fixed-budget algorithm would be interesting to study and a useful setting in practice. We hope to  
27 study it in follow up work. Naively, (ST)<sup>2</sup> could be altered to perform anytime fixed budget borrowing from techniques  
28 in [2] though this may not perform particularly well in practice and is not optimal. It is not immediately clear how to  
29 incorporate the ideas of FAREAST, specifically the technique in the Bad Filter, for an optimal fixed-budget algorithm  
30 and would be an interesting challenge for a future work.

31 **Reviewer 3:** Thank you for your kind review. We will correct the typos that you noted.

32 **Reviewer 4:** Thank you for taking the time to review our work. Regarding using the F1 score in experiments, F1  
33 equaling 1.0 is equivalent to an algorithm exactly identifying the set of all  $\epsilon$ -good arms correctly - the objective of  
34 this work. Visualizing the F1 score as a function of the number of samples serves to demonstrate the expected sample  
35 complexity of the algorithm until  $F1 \approx 1$ , and also provides a continuous measure of the performance of the algorithm.  
36 In particular, even if (ST)<sup>2</sup> has not yet found all  $\epsilon$ -good arms, it still achieves high F1 scores relative to other methods.  
37 Addressing the question about the correct probability directly, for synthetic experiments, we observed that the algorithms  
38 always correctly returned the set of all  $\epsilon$  good arms at termination. For the Caption Contest data experiments in Figure  
39 4a, we ran with  $\delta = .1$  and terminated at 10M pulls even if the stopping criteria had not been satisfied. In those  
40 experiments, we observed that in almost all ( $> 99\%$ ) cases, the F1 score of (ST)<sup>2</sup> was 1.0 around 10M pulls and beyond,  
41 indicating that the algorithm correctly identified all  $\epsilon$ -good arms by this point and would terminate correctly. Hence,  
42 (ST)<sup>2</sup> would achieve a correctness probability near 1 in this experiment - significantly better than  $1 - \delta = .9$ . In the  
43 case of the cancer dataset, we ran a small fraction to termination as well as with other values of  $\epsilon$ , and noted that the  
44 algorithm always returned the set correctly in all cases.

45 [1] Simchowitz, M., Jamieson, K., Recht, B. *The Simulator: Understanding Adaptive Sampling in the Moderate-Confidence*  
46 *Regime*. Conference on Learning Theory, 2017.

47 [2] Jun, K.S., Nowak, R. *Anytime Exploration for Multi-armed Bandits using Confidence Information*. International Conference  
48 on Machine Learning, 2016.